

Problem 1: Give state diagrams of NFAs recognizing the following languages. The alphabet is $\Sigma = \{0,1\}$.

- (a) $L_1 = \{w \mid \text{every odd position of } w \text{ is a } 1\}$
- (b) $L_2 = \{w \mid w \text{ contains an odd number of } 0\text{'s, or exactly two } 1\text{'s}\}$
- (c) $L_3 = \{w \mid w \text{ contains the substring "000"}\}$
- (d) $L_4 = \{w \mid w \text{ ends with "101"}\}$
- (e) $L_5 = \{w \mid w \text{ contains the substring "000" and ends with "101"}\}$
- (f) $L_6 = \{w \mid w \text{ is any binary string except "11101"}\}$

Problem 2: Give a regular expression for the following, and then convert the expressions to NFAs.

- (a) $A = \{w : w \text{ has two } 0\text{'s} \}$ where $\Sigma = \{0,1\}$
- (b) $B = \{w : w \text{ ends in "bbb"} \}$ where $\Sigma = \{a,b\}$
- (c) $C = \{w : w \text{ starts with "aa" and ends with any number of "b"s} \}$ where $\Sigma = \{a,b,c\}$
- (d) $D = \{w : w \text{ is a string representing an even binary number} \}$ where $\Sigma = \{0,1\}$

Problem 3: Design NFAs to recognize the following regular languages, and then convert the NFAs to DFAs.

- (a) $(a \cup b)^* abb(a \cup b)^*$
- (b) $((aa)^* (bb)) \cup ab)^*$
- (c) $(ab)^* a(ba)^*$
- (d) $(b(aaaaa)^* bb \cup bab)$
- (e) Give a description (english) of the languages accepted by (c) and (d).